Test form **422** 

Name (printed)

Recitation Section (see back of test):

# Honor Code Statement:

The work on this test reflects my individual problem-solving efforts, and has not been influenced by any information improperly obtained from another Georgia Tech student during the exam.

(signed)\_

- 1) Print your name, test form number (above), and nine-digit student number in the section of the answer card labeled "STUDENT IDENTIFICATION".
- 2) Bubble your test form number (ABOVE) in columns 1-3, skip column 4, then bubble in your student number in columns 5-13.



- 3) For each free-response question, show all relevant work supporting your answer. **Clearly box or underline your final answer.** "Correct" answers which are not supported by adequate calculations and/or reasoning will be counted wrong.
- 4) For each multiple-choice question, select the answer most nearly correct, **circle this answer on your test**, and bubble it in on your answer card. Show all relevant work on your quiz.
- 5) Be prepared to present your Buzzcard as you turn in your test. Scores will be posted to WebAssign after they have been been graded. Quiz grades become final when the next quiz is given.
- 6) You may use a simple scientific calculator capable of logarithms, exponentials, and trigonometric functions. **Programmable** engineering calculators with text or graphical capabilities are not allowed. Wireless devices are prohibited.



Our final exam will be on Wednesday, May 4 From 6:00 PM to 8:50 PM

# Your test form is: 422

The following problem will be hand-graded. <u>Show all your work for this problem</u>. Make no marks and leave no space on your answer card for it.

[I] (20 points) A spring is placed on a frictionless ramp that is inclined  $30^{\circ}$  above the horizontal. When a block of mass *m* is placed a distance *L* above the equilibrium position of the spring (top) and released, the block compresses the spring by a distance d = L/2 before stopping (bottom). If the block is <u>instead</u> released a distance 2L above the equilibrium position of the spring, how far *s* will the block compress the spring before stopping? Express *s* as a fraction of the original distance *L*.

[Hint: start by finding an expression for the spring constant k in terms of the parameters g, m, and L.]



The following problem will be hand-graded. <u>Show all your work for this problem</u>. Make no marks and leave no space on your answer card for it.

**[II]** (20 points) An empty sled of mass *m* is at rest on a level patch of rough snow having coefficient of friction  $\mu_k = 0.25$ . A child begins to push the sled, using an applied force P = 2mg directed at an angle  $\theta = 30^\circ$  below the horizontal. He pushes a total distance *D* in a staight line before letting go (and then hopping onto the sled, but that's not part of the problem...).

Draw a free body diagram for the sled while it is being pushed. *The quality of your diagram will be a graded part of this question!* Write out expressions for the work done by <u>every</u> force that acts on the sled. In each case, express the work in terms of D,  $g, m, \mu_k$ , and  $\theta$ . (If a particular force does <u>no</u> work, be sure to explain why it does so.)



Now, let D = 1.5 meters, and use the Work-Kinetic Energy Theorem to determine the final speed of the sled at the moment the child lets go.

The following problem will be hand-graded. <u>Show all your work for this problem</u>. Make no marks and leave no space on your answer card for it.

**[III]** (20 points) Two point masses (2m and 3m) are attached via a rigid, massless rod of length L, as shown at top right. A massless vertical axle is passed through the left end of the assembly (i.e. directly through mass 2m) as shown, and the whole assembly is given an angular speed  $\omega$ . The work required to cause this rotation, beginning from rest, is  $W_{left}$ . (Note: the Work-Kinetic Energy Theorem applies to rotations just as it applies to translations...)

Suppose instead that the vertical axle is passed through the <u>center of mass</u> of the assembly, as shown in the bottom figure. Determine the amount of work  $W_{CM}$  that would be required to give the new assemply the same rotational speed  $\omega$  (again starting from rest). Express your answer as a multiple (or fraction) of  $W_{left}$ .

You will need to start by locating the assembly's center of mass!



#### Question value 5 points

- (1) In the figures at right, four ojects (labelled by their masses) are acted upon by the indicated force vectors (labelled by their *magnitudes*), as the objects experience the indicated vector displacements (also labelled by *magnitudes*). Rank, from most positive to most negative, the work done on obects A–D by theses forces.
  - (a)  $W_A > W_C > W_B > W_D$
  - (b)  $W_A = W_C > W_B > W_D$
  - (c)  $W_D > W_C = W_A > W_B$
  - (d)  $W_D > W_B > W_A > W_C$
  - (e)  $W_C > W_A > W_D > W_B$



## Question value 5 points

- (2) A particle moves along the x-axis, subject only to a varying x-directed force, graphed at right as a function of position. How much work does the force do on the particle, as the particle moves between  $\vec{x} = 0$  and  $\vec{x} = \langle +D \rangle$ ?
  - (a)  $\frac{1}{2}F_{max}D$
  - (b)  $\frac{3}{4}F_{max}D$
  - (c)  $\frac{5}{8}F_{max}D$
  - (d)  $\frac{3}{5}F_{max}D$
  - (e)  $\frac{3}{8}F_{max}D$

#### Question value 5 points

- (3) A cable is used to winch a pallet of roofing tiles from ground level to the top of a five-story building. During this process, the <u>only</u> forces acting on the pallet are tension and gravity; there is no significant aerodynamic drag to consider. Consider the pallet while it is rising at constant speed, partway through the process. Describe the work done by tension,  $W_T$ , the work done by gravity,  $W_g$ , and the energy changes they cause.
  - (a)  $W_T$  is zero leaving the kinetic energy unchanged, while  $W_q$  is positive and adds to the potential energy.
  - (b)  $W_T$  is positive and adds to the mechanical energy, while  $W_g$  is negative and adds to the potential energy.
  - (c)  $W_T$  is positive and adds to the potential energy, while  $W_g$  is zero and leaves the mechanical energy unchanged.
  - (d)  $W_T$  is negative and subtracts from the mechanical energy, while  $W_g$  is positive and adds to the potential energy.
  - (e)  $W_T$  is and  $W_g$  are both zero, leaving the mechanical and potential energies unchanged...



#### Question value 5 points

(4) An object moving to the right is acted upon by a constant force such that the object experiences a leftward acceleration. What can be said about the power delivered to the object by the force?

- (a) The power is positively-valued, and remains constant as time passes.
- (b) The power is negatively-valued, and remains constant as time passes.
- (c) The power is positively-valued, and increases in magnitude as time passes.
- (d) The power is negatively-valued, and increases in magnitude as time passes.
- (e) The power is negatively-valued, and decreases in magnitude as time passes.

#### Question value 5 points

(5) A thin rod of mass M and length L, when rotated about an axis <u>through its endpoint</u>, has a moment of inertia  $I_{end} = ML^2/3$ . Starting with two identical rods, you create a 2-blade propellor by breaking one rod into two equal parts, and attaching their <u>ends</u> to a hub, and a 3-blade propellor by breaking the rod into three equal parts and attaching their <u>ends</u> to another hub. (Assume both propellor <u>hubs</u> have negligible mass.) Compare the moment of inertia of the 3-blade prop to the moment of inertia of the 2blade prop.

(a) 
$$I_3 = \frac{4}{9}I_2$$

(b) 
$$I_3 = \frac{3}{2}I_2$$

(c) 
$$I_2 = \frac{9}{-}I_2$$

(d) 
$$I_3 = I_2$$

(e) 
$$I_3 = \frac{2}{3}I_2$$



Question value 5 points

- (6) Tom stands at the top of a stairwell, and defines  $U_T = 0$  at his location. Ben stands at the bottom the same stairwell, and defines  $U_B = 0$  at his location. Tom tosses a soda can down to Bob. While it is in flight, what do Tom and Ben infer about the kinds of energy possessed by the can?
  - (a) Ben sees less kinetic energy and less total mechanical energy.
  - (b) Tom sees less kinetic energy, but more total mechanical energy.
  - (c) They both see the same kinetic energy, but Ben sees more total mechanical energy.
  - (d) They both see the same kinetic energy, but Tom sees more total mechanical energy.
  - (e) They both see the same kinetic energy and the same total mechanical energy

## The next two questions involve the following situation:

The picture at top right shows a schematic side view of a neutral atom trapped within a three-layer graphene film. (Graphene is simply a flat, hexagonally shaped sheet of carbon atoms.) Below that, the total potential energy of the atom is plotted as a function of the vertical position z within the tri-layer film. No external or dissipative forces act. The atom begins at position  $z_0$ .

## Question value 5 points

- (7) In which regions listed below would the atom experience a force in the *downward* (i.e. negative-z) direction? (If a <u>range</u> of positions is listed, the atom must experience a downward force at <u>all</u> positions within the given range.)
  - (a) Everywhere beyond position  $z_D$ .
  - (b) Between positions  $z_2$  and  $z_1$ .
  - (c) Between positions  $z_B$  and  $z_C$ .
  - (d) Between positions  $z_A$  and  $z_B$ .
  - (e) Only exactly <u>at</u> points  $z_A$ ,  $z_C$ , and  $z_D$ .





#### *Question value* 5 points

- (8) What <u>minimum</u> kinetic energy must the atom have at  $z_0$  to escape from the film? [Assume the film has infinite extent in the horizontal *x* and *y*-directions, so no motion in those directions allow a true <u>escape</u>.]
  - (a) The minimum kinetic energy for the atom to escape is  $K = E_0$ .
  - (b) There is no kinetic energy value for which the atom can escape.
  - (c) The minimum kinetic energy for the atom to escape is  $K = 3E_0$ .
  - (d) The minimum kinetic energy for the atom to escape is  $K = -E_0$ .
  - (e) The minimum kinetic energy for the atom to escape is  $K = 2E_0$ .

# PHYS 2211 B/C Recitation TA and Room Assignments

Tests will be returned in recitation, ideally in the <u>same</u> week as the test is given. In order to ensure that you receive your test back <u>as soon as possible</u>, please enter your recitation section from the table below on the front of this test.

	Clough 123	Clough 125	Clough 127	Clough 131	Clough 325
MONDAY					
2:05 – 2:55 pm		B05 Dark, Jason			B01 Coenen, Ashley
3:05 – 3:55 pm	C02 Eswar, Aditya				B02 Coenen, Ashley
4:05 – 4:55 pm	B06 Eswar, Aditya				B09/C01 Coenen, Ashley
TUESDAY					
2:05 – 2:55 pm					C03 Moreno, Maria
3:05 – 3:55 pm	B04 Dark, Jason				C09 Niranjan Babu, Siddarth
4:05 – 4:55 pm			B03 Dark, Jason	C04 Niranjan Babu, Siddarth	
WEDNESDAY					
2:05 – 2:55 pm					
3:05 – 3:55 pm	C05 Eswar, Aditya				
4:05 – 4:55 pm	C06 Eswar, Aditya				
THURSDAY					
2:05 – 2:55 pm					B08 Niranjan Babu, Siddarth
3:05 – 3:55 pm	B07 Lall, Sidharth				
4:05 – 4:55 pm			C08 Lall, Sidharth		
5:05 – 5:55 pm		C07 Walia, Saumya			