Name $\qquad$

Fall 2015

## Exam 4

$\qquad$

1) Print your name, test form number (above), and nine-digit student number in the section of the answer card labeled "STUDENT IDENTIFICATION".
2) Bubble your test form number (ABOVE) in columns 1-3, skip column 4, then bubble in your student number in columns 5-13.

3) For each free-response question, show all relevant work supporting your answer. Clearly box or underline your final answer. "Correct" answers which are not supported by adequate calculations and/or reasoning will be counted wrong.
4) For each multiple-choice question, select the answer most nearly correct, circle this answer on your test, and bubble it in on your answer card. Show all relevant work on your quiz.
5) Be prepared to present your Buzzcard as you turn in your test. Scores will be posted to WebAssign after they have been been graded. Quiz grades become final when the next quiz is given.
6) You may use a simple scientific calculator capable of logarithms, exponentials, and trigonometric functions. Programmable engineering calculators with text or graphical capabilities are not allowed. Wireless devices are prohibited.

Your test form is: 642


## Our Final Exam will be held on Monday, December 7 at 8:00am!

The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[I] (20 points) A block is released from rest on a ramp of height $h$. It slides without friction to the bottom of the ramp, and then continues across a horizontal frictionless surface, with a final speed $v$. A second identical block is released from the same height on a similar ramp. When it reaches the bottom of the ramp, it crosses a rough horizontal patch having length $d=3 \mathrm{~h}$. When it leaves the rough patch, it has a speed $v / 2$.

Use the General Work-Energy Principle to find the coefficient of friction of the rough patch.


The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[II] (20 points) A string is wrapped around a pulley wheel of mass $m$ and radius $R$, as shown in the figure. The pulley can rotate freely about its axle, without any friction. The loose end of the string is attached to a block of mass 2 m . You may assume that the spokes of the pulley wheel have negligible mass, so that it may be treated an ideal hoop, with $I_{\mathrm{cm}}=m R^{2}$.

Find an expression for the tension in the cord when the block is released. Express your answer as a multiple of $m g$.


The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[III] (20 points) A hinged beam of weight $W$ is attached to a vertical wall, supported in equilibrium by a cable that is attached to the wall above the hinge point. The beam is oriented at a $30^{\circ}$ angle above the horizontal, while the cable is directed at an angle of $30^{\circ}$ below the horizontal. Determine the Tension $T$ in the cord, as well as the magnitude and direction of the force $\vec{H}$ exerted by the hinge on the beam.

Express both force magnitudes as multiples of the beam's weight W. Express the direction of $\vec{H}$ as an angle $\phi$ relative to the horizontal


Question value 5 points
(1) A hoop ( $I_{\mathrm{cm}}=m r^{2}$ ) and a uniform disk $\left(I_{\mathrm{cm}}=\frac{1}{2} M R^{2}\right)$ are both rolling without slipping along a horizontal surface, when they encounter an upward ramp. Which of the two objects will roll to the highest point on the ramp,
 before stopping?
(c) The object with the greater radius will roll the highest.
(b) The disk will roll the highest, regardless of mass or radius.
(c) The object with the greater mass will roll the highest.
(d) The hoop will roll highest, regardless of mass or radius.
(e) They will roll to the same height, regardless of mass or radius.

Question value 5 points
(2) A conservative force, acting alone, does negative work on an object. As a result of this work,
(a) ...the potential energy decreases and the total mechanical energy increases.
(b) ...the potential energy increases and the total mechanical energy decreases.
(c) ...the potential energy increases and the total mechanical energy does not change.
(d) ...the potential energy does not change and the total mechanical energy decreases.
(e) ...the potential energy decreases and the total mechanical energy does not change.

Question value 5 points
(3) The graphs at right displays the potential energy curve for a conservative force that acts on a particle that is otherwise free to move along the $x$-axis. In which of the regions shown is the particle experiencing a force in the negative $x$-direction?
(a) In regions II and III.
(b) In regions I and IV.
(c) In regions III and IV.

(d) In none of the regions shown.
(e) In regions I and II.

The next two questions involve the following situation:
A non-uniform rod of mass $M$ and length $L$ lies along the $x$-axis, extending from $x=0$ to $x=L$. The rod is characterized by a linear mass density that satisfies the expression:

$$
\lambda(x)=\frac{2 M}{3 L}\left(1+\frac{x}{L}\right) \quad \text { for } \quad 0 \leq x \leq L
$$

Question value 5 points
(4) What is the $x$-coordinate of the rod's center of mass?
(a) $\quad x_{\mathrm{cm}}=\frac{1}{2} L$
(b) $x_{\mathrm{cm}}=\frac{2}{3} L$
(c) $\quad x_{\mathrm{cm}}=\frac{4}{9} L$
(d) $x_{\mathrm{cm}}=\frac{3}{5} L$
(e) $\quad x_{\mathrm{cm}}=\frac{5}{9} L$

Question value 5 points
(5) Lamar, Chloe, and Ralph each have identical copies of the rod described above. Lamar sets a perpendicular pivot axis through the rod at the left end $(x=0)$. Chloe sets a perpendicular pivot axis through the center of mass. Ralph sets a perpendicular pivot axis through the right end of the rod. Starting from rest, all three rods are then spun up to the same final angular speed, $\omega$. Rank, from greatest to least the work that is required to cause each of there rotations.
(a) $W_{L}>W_{R}>W_{C}$
(b) $W_{C}>W_{R}>W_{L}$
(c) $W_{L}=W_{R}=W_{C}$
(d) $W_{R}>W_{L}>W_{C}$
(e) $W_{C}>W_{L}=W_{R}$

The next two question involve the following situation:
Object A has mass $m$ and object B has mass $2 m$. Starting from rest, both objects are pushed in a straight line along a frictionless surface by force of magnitude $F$.

Question value 5 points
(6) Suppose that both objects are pushed through the same total distance $D$ by the force. Compare the work done on objects A and B by force $F$, and also compare the (magnitude of) impulse delivered to objects A and B by force $F$.
(a) $W_{B}>W_{A}$ and $J_{B}=J_{A}$
(b) $\quad W_{B}<W_{A}$ and $J_{B}>J_{A}$
(c) $\quad W_{B}=W_{A}$ and $J_{B}=J_{A}$
(d) $\quad W_{B}>W_{A}$ and $J_{B}<J_{A}$
(e) $\quad W_{B}=W_{A}$ and $J_{B}>J_{A}$

Question value 5 points
(7) Suppose instead that both objects are pushed for the same total time $\Delta t$ by the force. Compare the work done on objects A and B by force $F$, and also compare the (magnitude of) impulse delivered to objects A and B by force $F$.
(a) $\quad W_{B}=W_{A}$ and $J_{B}=J_{A}$
(b) $\quad W_{B}>W_{A}$ and $J_{B}>J_{A}$
(c) $\quad W_{B}=W_{A}$ and $J_{B}<J_{A}$
(d) $\quad W_{B}<W_{A}$ and $J_{B}=J_{A}$
(e) $\quad W_{B}<W_{A}$ and $J_{B}>J_{A}$

Question value 5 points
(8) A baseball is thrown straight upward with a large initial speed $v$. The instantaneous power delivery to the baseball by gravity, as the ball rises to its highest point, is:
(a) constant and positive throughout the ball's rise.
(b) negative throughout the ball's rise, intially very large but gradually dropping to zero.
(c) initially zero, but gradually increaing to a large negative value as the ball rises.
(d) always zero, because no power is ever delivered by a conservative force like gravity.
(e) constant and negative throughout the ball's rise

## PHYS 2211 A/B Recitation TA and Room Assignments

Tests will be returned in recitation, ideally in the same week as the test is given. In order to ensure that you receive your test back as soon as possible, please enter your recitation section from the table above on the front of this test.

|  | Clough 123 | Clough 125 | Clough 127 | Clough 131 |
| :--- | :--- | :--- | :--- | :--- |
| Wednesday |  |  |  |  |
| $1: 05-1: 55 \mathrm{pm}$ | B01 Dark, Jason |  |  |  |
| $2: 05-2: 55 \mathrm{pm}$ |  | A01 Coenen, Ashley |  |  |
| $3: 05-3: 55 \mathrm{pm}$ |  |  | B06 Coenen, Ashley | A05 Cowan, Erika |
| $4: 05-4: 55 \mathrm{pm}$ | B05 Eswar, Aditya | B02 Dark, Jason | A02 Coenen, Ashley | A06 Cowan, Erika |
| ThuRsDAY |  |  |  |  |
| $1: 05-1: 55 \mathrm{pm}$ |  |  | B03 Dark, Jason |  |
| $2: 05-2: 55 \mathrm{pm}$ | A03 Eswar, Aditya | B08 Cowan, Erika | A07/B07 Dark, Jason |  |
| $3: 05-3: 55 \mathrm{pm}$ |  |  | B04 Dark, Jason |  |
| $4: 05-4: 55 \mathrm{pm}$ | A04 Eswar, Aditya |  | A08 Dark, Jason |  |
| $5: 05-5: 55 \mathrm{pm}$ |  |  |  |  |

