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Spring 2016

## Exam 3

Recitation Section (see back of test):

1) Print your name, test form number (above), and nine-digit student number in the section of the answer card labeled "STUDENT IDENTIFICATION".
2) Bubble your test form number (ABOVE) in columns 1-3, skip column 4, then bubble in your student number in columns 5-13.

3) For each free-response question, show all relevant work supporting your answer. Clearly box or underline your final answer. "Correct" answers which are not supported by adequate calculations and/or reasoning will be counted wrong.
4) For each multiple-choice question, select the answer most nearly correct, circle this answer on your test, and bubble it in on your answer card. Show all relevant work on your quiz.
5) Be prepared to present your Buzzcard as you turn in your test. Scores will be posted to WebAssign after they have been been graded. Quiz grades become final when the next quiz is given.
6) You may use a simple scientific calculator capable of logarithms, exponentials, and trigonometric functions. Programmable engineering calculators with text or graphical capabilities are not allowed. Wireless devices are prohibited.

Your test form is: 363


## Our next test will be on Monday, April 11!

The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[I] (20 points) A worker of mass $m$ is trying to use a rope to pull a large block of ice (having mass $M=2 \mathrm{~m}$ ) up a ramp that is inclined at an angle $\theta=27^{\circ}$ above the horizontal. Unfortunately, there is not enough traction, so the worker and block begin to slide down the ramp. The coefficient of kinetic friction between the worker and the ramp is $\mu_{\mathrm{k}}=0.42$, and friction between the block and the ramp is negligible.


Construct free body diagrams for both the worker and the block, decompose any force vectors that are not along your cartesian axes, and then write out statements of the second law for each object. The quality of your diagrams will be graded!

Use your expressions to determine the magnitude of acceleration, $a$, for the block and the worker, and then find the magnitude of the tension force in the rope. Express the acceleration as a multiple of $g$, and the tension as a multiple of the worker's actual weight, mg.

The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[II] (20 points) Modern roller coasters have vertical loops with a small radius of curvature at the top (to keep the inverted passengers pressed into their seats), and a large radius of curvature at the bottom (to prevent the passengers from being pressed too firmly into their seats). Consider the double-loop at right, with a radius of curvature $R$ at the top, and a radius of curvature $3 R$ at the bottom.

When a passenger passes through the top of the loop (position T) moving at a speed $v_{\mathrm{T}}$, she feels that she is pressed into her seat with an apparent force equal to her true weight, $m g$. When she passes through the bottom
 of the loop (position B), she feels that she is pressed into her seat with an apparent force equal to three times her true weight.

Determine the speed $v_{\mathrm{B}}$ of the roller-coaster car as it passes through the bottom of the loop, expressed as a multiple of $v_{\mathrm{T}}$.

The following problem will be hand-graded. Show all your work for this problem. Make no marks and leave no space on your answer card for it.
[III] (20 points) Two identical sportscars (having masses $m$ ) collide at an intersection. The first is initially travelling due east at speed $v$, and the second is initially travelling due north at speed $2 v$. Immediately after the collision, the first car is observed to be skidding in a direction $\theta_{1}=36.9^{\circ}$ north of east, with a speed $2 v$.

Determine the velocity of the second car immediately after the collision. Express your answer first as a Cartesian component vector, then as a magnitude and direction relative to N/S/E/W axes.

[III+] (4 points extra credit) Immediately after the collision, what is the velocity of the second car, relative to the first car? Express your answer first as a Cartesian component vector, then as a magnitude and direction relative to N/S/E/W axes.

Question value 5 points
(1) A book rests atop a table, which rests on the floor of an elevator that is accelerating downwards. According to the $3^{\text {rd }}$ Law, what force (if any) is paired with the normal force exerted by the table on the book?
(a) The gravitational force by the Earth on the book.
(b) The normal force by the book on the table.
(c) Because the book and table are accelerating, they are not subject to the $3^{\text {rd }}$ Law
(d) The gravitational force by the Earth on the table.
(e) The normal force by the elevator floor on the table.


Question value 5 points
(2) Three identical cars drive around three different circular tracks. (All three tracks are level and unbanked.) Car $A$ drives on a dry track (coefficient of static friction $=\mu$ ) of radius $R$. Car $B$ drives around a dry track (coefficient of static friction $=\mu$ ) of radius $R / 2$. Car $C$ drives around an wet track (coefficient of static friction $=\mu / 3$ ) of radius $3 R$. Rank, from greatest to least, the top speeds that each car can attain, without skidding. [Hint: solve once using generic $R$ and $\mu-$ then consider how $\underline{\text { different }} R$ and $\mu$ values will effect $v_{\max }$.]
(a) $v_{A}=v_{C}>v_{B}$
(b) $v_{C}>v_{A}>v_{B}$
(c) $v_{B}>v_{A}=v_{C}$
(d) $v_{A}=v_{B}>v_{C}$
(e) $v_{B}>v_{A}>v_{C}$

Question value 5 points
(3) A hockey puck on frictionless ice has two tiny rocket motors glued to its top, pointing in opposite directions. The puck is given a push in a direction perpendicular to the rockets' orientations. As the puck crosses line A, the leftward-firing rocket is ignited, burning out as the puck crosses line B. As the puck crosses line C, the rightwardfiring rocket ignites, burning out as the puck crosses line D . The two rockets are identical. Which of the trajectories below best characterizes the motion of the puck?


(a)

(b)

(c)

(d)

(e)

The next two questions involve the following situation:
Blocks A, B and C are stacked as shown at right, on a frictionless surface. Their relative masses are $m_{A}=2 M, m_{B}=M$, and $m_{C}=3 M$. When block B is pulled to the right by a force $P$, all three blocks move together, without slipping relative to each other. (That is, they do slip collectively along the surface.)


Question value 5 points
(4) What is the magnitude of the friction force by block $B$ on block $C$ ?
(a) $f_{B C}=\frac{1}{3} P$
(b) $f_{B C}=\frac{2}{3} P$
(c) The force magnitudes cannot be determined without knowing the coefficientsof friction $\mu_{B C}$.
(d) $f_{B C}=\frac{5}{6} P$
(e) $f_{B C}=\frac{1}{2} P$

Question value 5 points
(5) What are the directions of the two friction forces on block B?
(a) Friction by A on B is to the right and friction by C on B is to the left.
(b) The force directions cannot be compared without knowing the coefficients of friction, $\mu_{A B}$ and $\mu_{B C}$.
(c) Friction by A on B is to the left and friction by C on B is to the left.
(d) Friction by A on B is to the right and friction by C on B is to the right.
(e) Friction by A on B is to the left and friction by C on B is to the right.

Question value 5 points
(6) Two identical blocks are at rest on a frictionless surface. Block $A$ is subjected to a force along the positive $x$-direction, of time-dependent magnitude $F_{A}$ graphed at right, while block B is subjected to a force along the $x$-direction of time-dependent magnitude $F_{B}$. Compare the magnitude of impulse delivered to block $A$ to the magnitude of impulse delivered to block B.

(a) $J_{B}=\frac{3}{2} J_{A}$
(b) $J_{B}=J_{A}$
(c) $J_{B}=2 J_{A}$
(d) $J_{B}=\frac{1}{2} J_{A}$
(e) $J_{B}=3 J_{A}$

## Question value 5 points

(7) In the figure at right, the eight cardinal compass directions split the map into octants (each subtending a $45^{\circ} \mathrm{arc}$ ): $\mathrm{Ia} / \mathrm{Ib}$, $\mathrm{IIa} / \mathrm{IIb}$, $\mathrm{IIIa} / \mathrm{IIIb}$, and $\mathrm{IVa} / \mathrm{IVb}$. Consider a car of mass $m$ is initially travelling due east with speed $v$. It speeds up while turning right, ending up moving due south with a speed $2 v$. Consider the vector impulse $\vec{J}$ delivered to the car during this process. The direction of $\vec{J}$ lies in which octant?
(a) $\vec{J}$ lies in octant IIIb.
(b) Impulse cannot be determined because the elapsed time was not specified.

(c) $\vec{J}$ lies in octant IIIa.
(d) $\vec{J}$ lies in octant IVa.
(e) $\vec{J}$ lies in octant IIa.

Question value 5 points
(8) In the figure at right, block $A$ overtakes block $B$. The resulting collision is perfectly inelastic. What will be the final velocity of block A, after the collision?
(a) $\vec{v}_{A f}=\langle+2 v\rangle$
(b) $\vec{v}_{A f}=\left\langle+\frac{2}{3} v\right\rangle$

(c) $\vec{v}_{A f}=\langle+v\rangle$
(d) $\quad \vec{v}_{A f}=\left\langle+\frac{3}{2} v\right\rangle$
(e) $\vec{v}_{A f}=\left\langle+\frac{4}{3} v\right\rangle$

## PHYS 2211 B/C Recitation TA and Room Assignments

Tests will be returned in recitation, ideally in the same week as the test is given. In order to ensure that you receive your test back as soon as possible, please enter your recitation section from the table below on the front of this test.

|  | Clough 123 | Clough 125 | Clough 127 | Clough 131 | Clough 325 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Monday |  |  |  |  |  |
| 2:05-2:55 pm |  | B05 Dark, Jason |  |  | B01 Coenen, Ashley |
| 3:05-3:55 pm | C02 Eswar, Aditya |  |  |  | B02 Coenen, Ashley |
| 4:05-4:55 pm | B06 Eswar, Aditya |  |  |  | B09/C01 Coenen, Ashley |
| Tuesday |  |  |  |  |  |
| $2: 05-2: 55 \mathrm{pm}$ |  |  |  |  | C03 Moreno, Maria |
| 3:05-3:55 pm | B04 Dark, Jason |  |  |  | C09 Niranjan Babu, Siddarth |
| 4:05-4:55 pm |  |  | B03 Dark, Jason | C04 Niranjan Babu, Siddarth |  |
| Wednesday |  |  |  |  |  |
| 2:05-2:55 pm |  |  |  |  |  |
| 3:05-3:55 pm | C05 Eswar, Aditya |  |  |  |  |
| 4:05-4:55 pm | C06 Eswar, Aditya |  |  |  |  |
| Thursday |  |  |  |  |  |
| $2: 05-2: 55 \mathrm{pm}$ |  |  |  |  | B08 Niranjan Babu, Siddarth |
| 3:05-3:55 pm | B07 Lall, Sidharth |  |  |  |  |
| 4:05-4:55 pm |  |  | C08 Lall, Sidharth |  |  |
| 5:05-5:55 pm |  | C07 Walia, Saumya |  |  |  |

